Given $f^{\prime}(x)=(1-x)(4-x)$, determine the intervals on which $f(x)$ is increasing or
decreasing.
Decreasing $(-\infty, 1)$; increasing on $(4, \infty)$
Increasing $(-\infty,-1) \cup(-4, \infty)$; increasing on $(-1,-4)$
Decreasing $(-\infty, 1) \cup(4, \infty)$; increasing on $(1,4)$
Decreasing $(1,4)$; increasing on $(-\infty, 1) \cup(4, \infty)$

Jan 7th 12:57:22 am

## Welcome back : Kara

Jan 7th 12:57:24 am

I'm finding you a tutor ASAP.
Jan 7th 12:57:26 am

BTW, the tutor will spend a minute reviewing your problem so when the session begins, you can quickly jump into it! Remember the tutor might still have questions about where and why you are stuck.

Jan 7th 12:57:28 am

Jan 7th 12:57:31 am

## Did you start on the problem, even just a little?

Jan 7th 12:57:34 am

If so, take a your work so I can send it to the tutor. There's no such thing as sending too little work $\because$
Jan 7th 12:57:36 am

No worries $\because$ your tutor can help you from the beginning!
Jan 7th 12:57:42 am

Sounds good
Jan 7th 12:57:44 am

TUTOR FOUND, NOW REVIEWING PROBLEM AT NO CHARGE

> Jan 7th 12:57:45 am

## Want to hear a Pro Yup Tip?...Yes? 11

Jan 7th 12:57:47 am

## All Yup tutors are real people, so please treat them with respect.

Jan 7th 12:57:50 am

Jan 7th 12:57:59 am

## Okay looks like you're ready to go :-

Jan 7th 12:58:06 am

SESSION STARTED AT 8:58 PM
Jan 7th 12:58:07 am

## Hello Kara, I am Usha your math tutor for the session!

Jan 7th 12:58:28 am $\checkmark \quad$ Introduction: Tutor greets student by name and introduces herself
I got your question on increasing and decreasing intervals and am pleased to help you with the same :)
Jan 7th 12:58:56 am $\checkmark$ Introduction: Builds rapport with reassuring language

How far have you gotten in solving the problem?
Jan 7th 12:59:11 am $\checkmark$ A1: Determine progress

Thank you I just got confused because when I graph this how the problem is I can't seem to find the answer so I was

## No worries! I can guide you on solving the problem using the derivative function given! <br> Jan 7th 1:00:29 am $\checkmark \quad$ C2: Reassure the student

[^0]Jan 7th 1:01:57 am

Any idea on how to use the derivative to determine the increasing and decreasing functions?
Jan 7th 1:02:07 am $\checkmark$ A1: Probe the student's understanding of concepts

What happens to the derivative when the function is increasing?
Jan 7th 1:02:27 am $\checkmark$ A1: Probe the student's understanding of concepts

Jan 7th 1:03:03 am $\checkmark$ B1/C1: Redirect student error

Let me send in the simple rule we use!
Jan 7th 1:03:11 am $\checkmark \quad$ C1: Adapt instruction to student gap

## $f^{\prime}(x)>0$ position

## $f(x)$ is increasing

Jan 7th 1:03:40 am $\checkmark \quad$ B2: Uploads relevant supporting information to supplement explanation

When the derivative $f^{\prime}(x)$ is positive $f(x)$ is increasing!
Jan 7th 1:03:54 am $\checkmark \quad$ C1: Adapt instruction to student gap

```
Same way, can you now guess when it is decreasing?
Jan 7th 1:04:10 am v C3: Invite student input
And negative decreasing
Jan 7th 1:04:16 am
```


## Fantastic!

```
Jan 7th 1:04:21 am \(\checkmark \quad\) C2: Encouraging language
```

So, to determine the intervals we first find the critical numbers!
Jan fth 1:04:41 am $\checkmark \quad$ B2: Explain approach upfront

```
That is we first find }x\mathrm{ , when f}\mp@subsup{f}{}{\prime}(x)=0\mathrm{ !
Jan 7th 1:05:05 am v B2: Clarifies step further
Can you try finding the critical values?
Jan 7th 1:05:17 am \(\checkmark \quad\) C3: Encourage student to take the next step
```


## That is cool:)

Jan 7th 1:06:02 am

Yes I'll try now
Jan 7th 1:05:52 am

Jan 7th 1:06:49 am $\vee \quad$ C2: Acknowledge student's mistake without causing stress

## How did you get these numbers?

Jan 7th 1:07:01 am $\checkmark \quad$ C2: Asks student to justify their thought process

## Yes! That was indeed done correct!

Jan 7th 1:07:44 am $\vee$ C2: Reassuring language Note: should be "...done correctly"

```
1-x=0. Then }x=\mathrm{ ?
Jan 7th 1:07:50 am v C3: Guiding question
```

So, what are the critical numbers?
Jan 7th 1:08:32 am $\checkmark \quad$ C3: Invite student input

Oh so 4 and 1
Jan 7th 1:08:36 am

> Awesome :) You fixed it quick!
> Jan 7th 1:08:50 am $\checkmark \quad$ C2: Reassuring language

We now need to analyze the intervals formed by these two numbers on number line!
Jan 7th 1:09:31 am $\checkmark \quad$ B2: Guide student towards next step

What are the intervals formed?
Jan 7th 1:09:39 am $\checkmark \quad$ C3: Invite student input

## C1: Adapts explanation to student's confusion

Not yet to that! Let me show the intervals formed on the number line! Just one moment!
Jan 7th 1:10:33 am


Jan 7th 1:11:05 am $\checkmark \quad$ B2: Supplements explanation with visual aid

We have three intervals formed!
Jan 7th 1:11:21 am

Values less than 1 or (-inf, 1)
Jan 7th 1:11:33 am

Values between 1 and 4 or $(1,4)$
Jan 7th 1:11:45 am

And finally values greater than 4 (4,inf)
Jan 7th 1:11:58 am

Cool:) We now need to check the sign of $f^{\prime}(x)$ in these intervals!
Jan 7th 1:12:17 am $\checkmark \quad$ B2: Guide student towards next step
We can use test values to do that!

Jan 7th 1:12:27 am

Let us take the first interval (-inf, 1)
Jan 7th 1:12:44 am

```
Fantastic! You chose the right and easiest one!
Jan 7th 1:13:33 am \checkmark C2: Encouraging language
```


## What do we get for $f^{\prime}(0)$ ?

```
Jan 7th 1:13:45 am \(\checkmark \quad\) C3: Guiding question
```


## Correct! That means $f^{\prime}(x)$ is positive in (-inf,1). Right?

Jan 7th 1:14:39 am $\checkmark \quad$ B2: Breaks down concept further


Jan 7th 1:14:46 am $\checkmark \quad$ B2: Supplements steps with visual aid to allow student to follow their progress

So we choose a number between 1 and 4 ?
Jan 7th 1:15:29 am

## Yes! Go ahead :)

Jan 7th 1:15:38 am $\quad \checkmark \quad$ C3: Invite student to proceed independently


Jan 7th 1:16:32 am


Jan 7th 1:16:48 am

Awesome :) You got the signs correct
Jan 7th 1:16:57 am $\checkmark \quad$ C2: Positive language

I guess you can now find the increasing and decreasing intevals!
Jan 7th 1:17:19 am $\checkmark \quad$ C3: Invite student to proceed independently

Yes so the last one
Jan 7th 1:17:55 am


Jan 7th 1:18:07 am

Woohoo! You are right :)
Jan 7th 1:18:27 am $\checkmark \quad$ C2: Positive language

Thanks this makes a lot more sense
Jan 7th 1:18:42 am

Can you now summarize what we do to find the decreasing and increasing intervals!
Jan 7th 1:18:54 am $\checkmark \quad$ B2/C1: Tutor invites student to summarize key ideas to cement learning, check for understanding

```
It is just to check you got the concept correct :)
```

Jan 7th 1:19:06 am

Yes first we find the critical points then plot them on the graph and then test whether there negative or positive to see if there increasing or decreasing

Jan 7th 1:19:47 am

[^1]Increasing if it is positive and decreasing if negative!
Jan 7th 1:20:20 am $\checkmark \quad$ B2: Recap to ensure understanding

```
I appreciate your patience and sincerity in learning things correct!
Jan 7th 1:20:40 am V Praises student for their efforts and participation
    (Note: This should be phrased "...learning things correctly")
Is there anything else I can guide you on?
Jan 7th 1:20:49 am \checkmark Tutor checks to see if the student needs further help
You are welcome!
Jan 7th 1:21:13 am
Thank you for being with us at Yup!
Jan 7th 1:21:21 am \(\checkmark\) Conclusion: Tutor thanks student for using Yup
```


## Bye for now and take care!

```
Jan 7th 1:21:26 am \(\checkmark\) Conclusion: Warm send off
```


[^0]:    What is given is the derivative function $f^{\prime}(x)$ !
    Jan 7th 1:00:57 am

    Had the function $f(x)$ is directly given, you can use the graph to sovle the problem!
    Jan 7th 1:01:23 am
    $\checkmark$ B1/C1: Redirect student error
    Note: this should be "Had the function $f(x)$ been directly given, you could use the graph to solve..."

    The (1-x)(4-x) should I solve this
    Jan 7th 1:01:50 am

    And oh that makes sense

[^1]:    Yes correct!
    Jan 7th 1:20:08 am $\quad \checkmark \quad$ C2: Positive language

